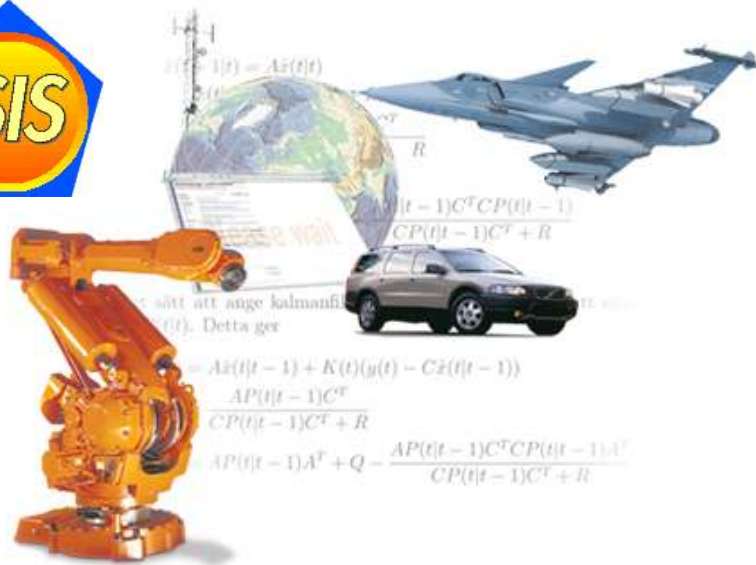


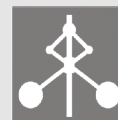
# Particle Filtering in Practice

Sensor fusion, Positioning and Tracking



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Map-Aided Positioning

Target Tracking

Positioning

Collision Avoidance

Analysis



## ▪ Positioning

- Robot positioning
- Map-Aided navigation
  - Underwater Navigation
  - Surface Navigation

## ▪ Analysis

- Quantization
- Complexity Analysis -- Marginalization



# Particle Filtering in Practice

- General model

$$x_{t+1} = f(x_t, w_t)$$

Process noise

$$y_t = h(x_t, e_t)$$

Measurement noise

- Common models for tracking and navigation

$$x_{t+1} = A_t x_t + w_t$$

$$y_t = h(x_t) + e_t$$



# Bayesian Recursions

$$p(x_t|Y_t) = \frac{p(y_t|x_t)p(x_t|Y_{t-1})}{p(y_t|Y_{t-1})}$$

$$p(y_t|Y_{t-1}) = \int_{\mathbb{R}^n} p(y_t|x_t)p(x_t|Y_{t-1})dx_t$$

Particle Filter

Extended Kalman Filter



# Robot Positioning & Sensor Fusion

R. Karlsson & M. Norrlöf



# Estimation Model

$$x_t = \begin{pmatrix} q_{a,t} & \dot{q}_{a,t} & \ddot{q}_{a,t} \end{pmatrix}$$

$$x_{t+1} = F_t x_t + G_{u,t} u_t + G_{w,t} w_t$$

$$y_t = h(x_t) + e_t$$

$$h(x_t) = \begin{pmatrix} q_{m,t} \\ \ddot{\rho}_t \end{pmatrix}$$

← Motor angle

← Cartesian acceleration

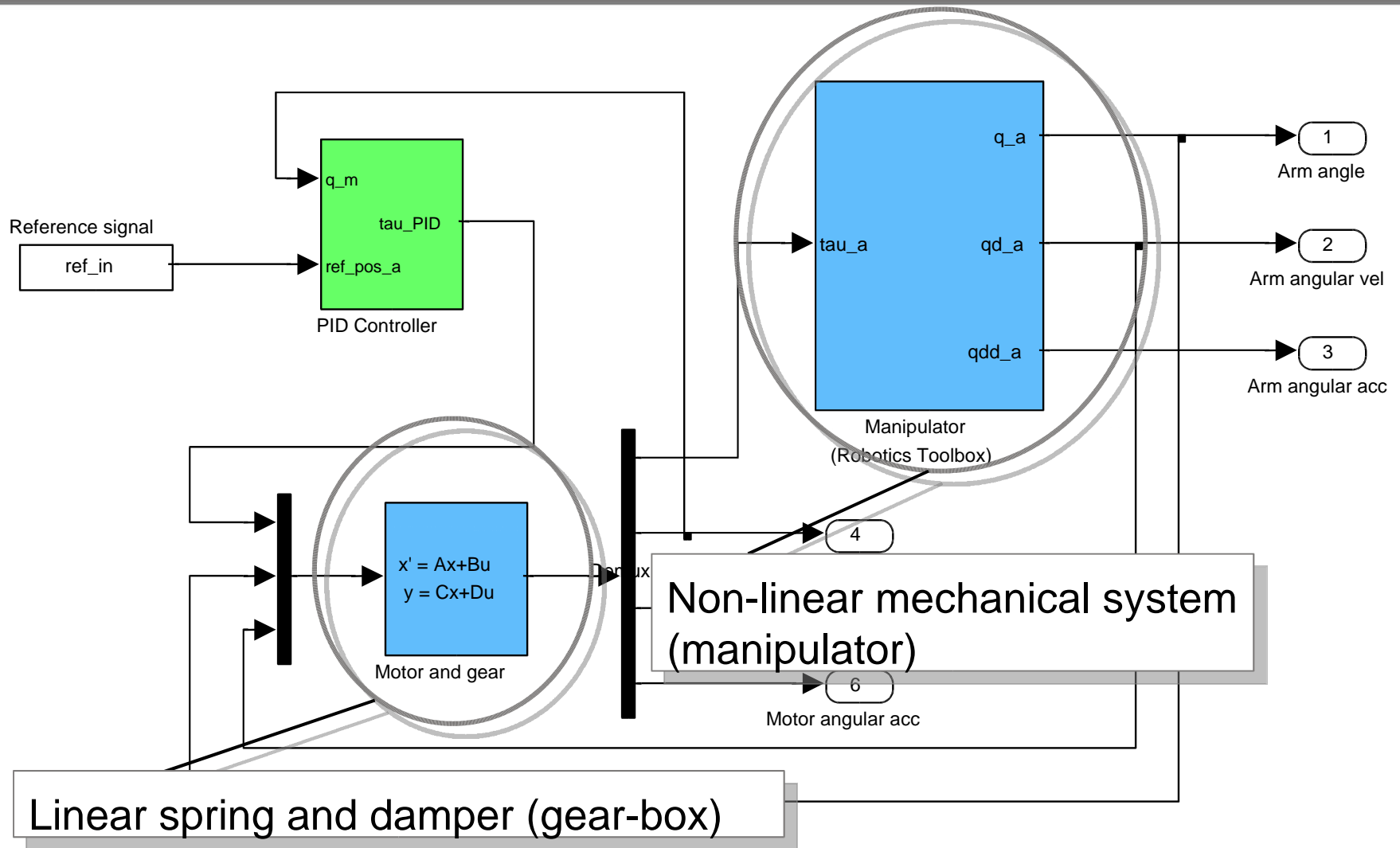
Sensor fusion based on Bayesian techniques



Accelerometer



# The "True" System





# Motivation: state estimation

$$q_m = \frac{1}{r_g} \left( q_a + \frac{1}{k} \left( \underbrace{M_a(q_a)\ddot{q}_a}_{\text{Inertia}} + \underbrace{C(q_a, \dot{q}_a)\dot{q}_a}_{\text{Coriolis}} + \underbrace{g(q_a)}_{\text{Gravity}} \right) \right)$$

Arm estimates

needed!

$$\hat{q}_{a,t}, \hat{\dot{q}}_{a,t}, \hat{\ddot{q}}_{a,t}$$

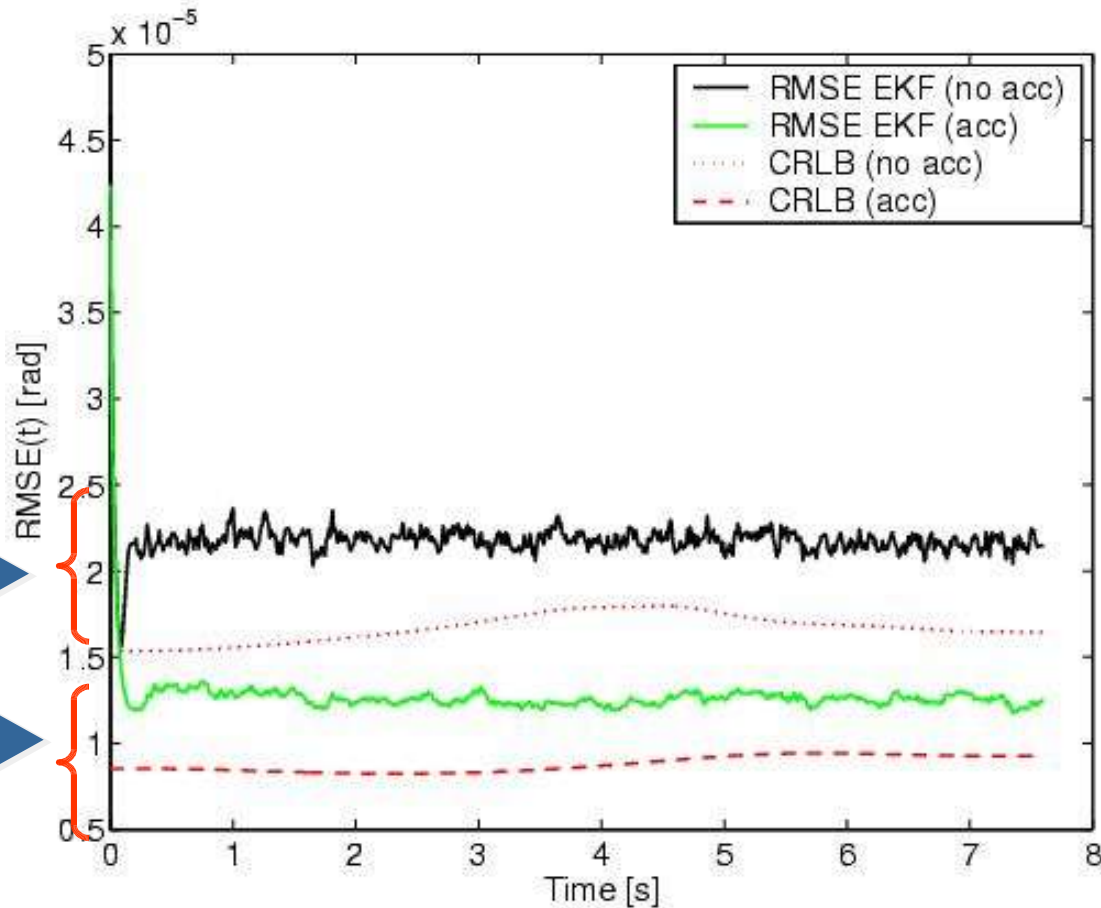


# EKF: RMSE and Cramér-Rao Lower Bound

No  
accelerometer



Accelerometer



# Underwater Navigation

R. Karlsson & F. Gustafsson



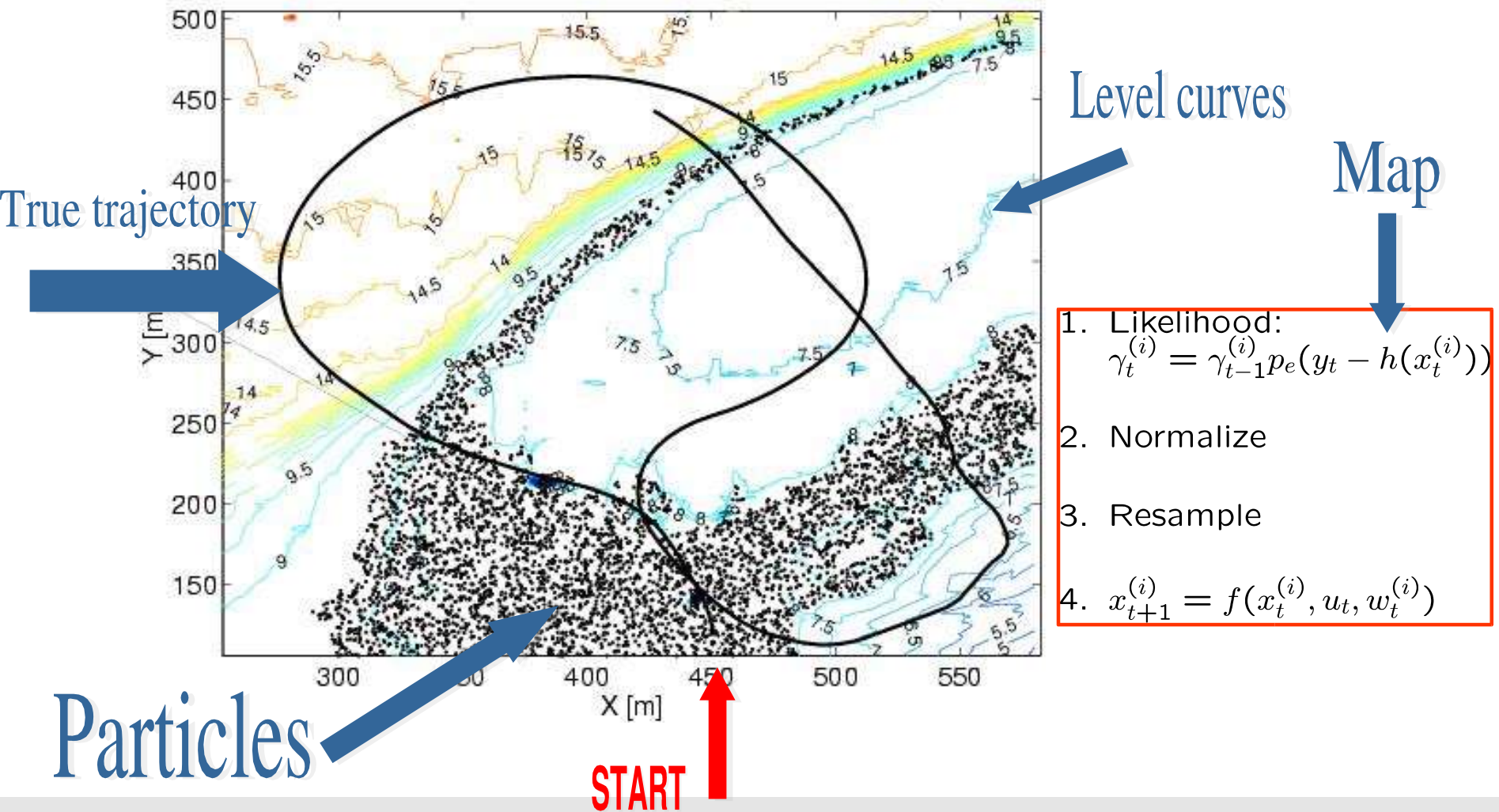
# Underwater Navigation

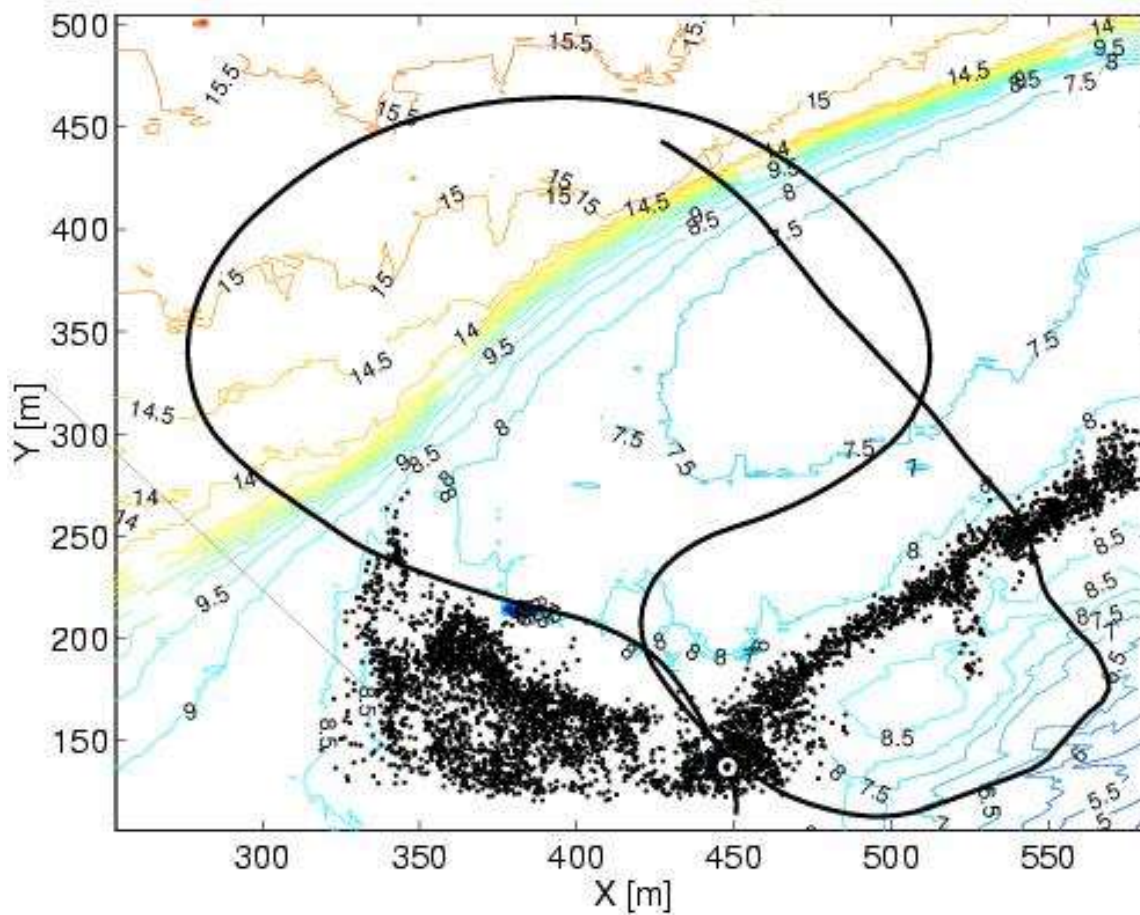
## Saab Bofors Underwater Systems

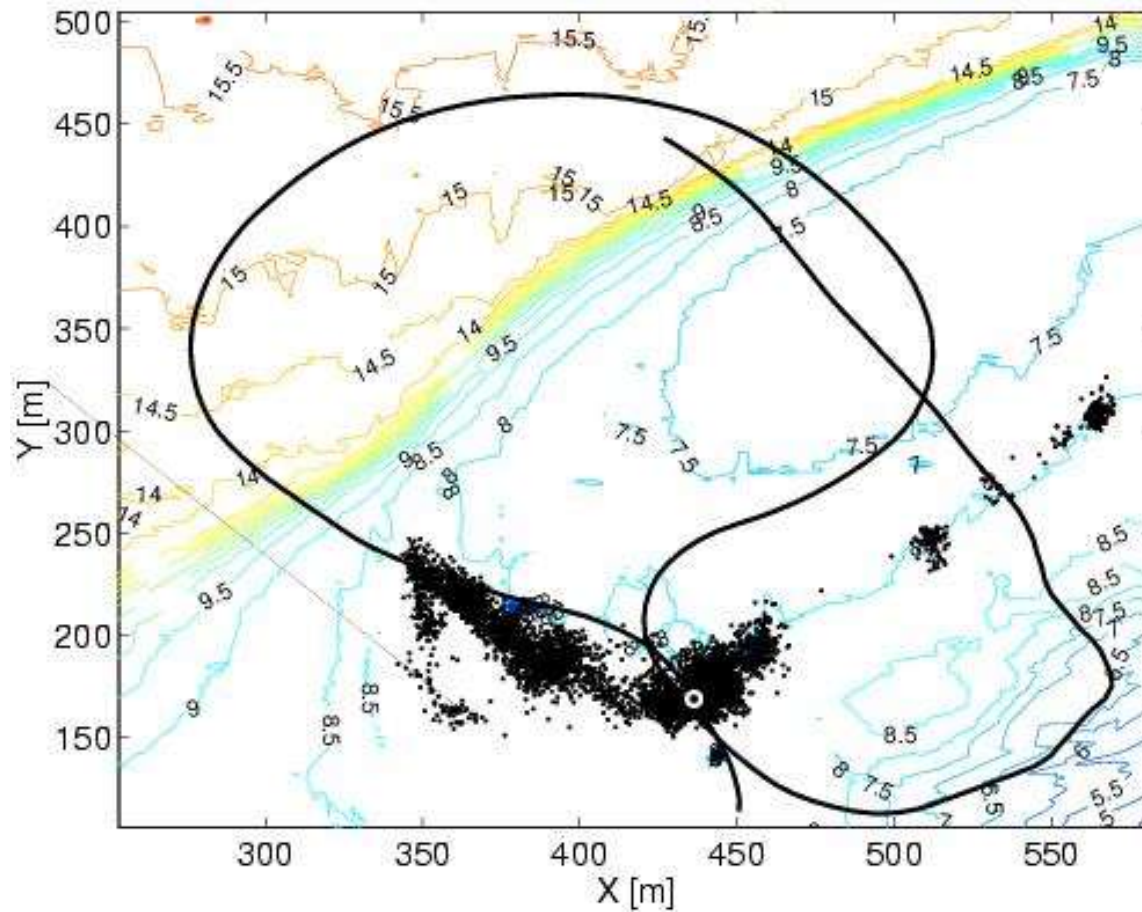
- Sonar depth sensor
- Depth map
- INS



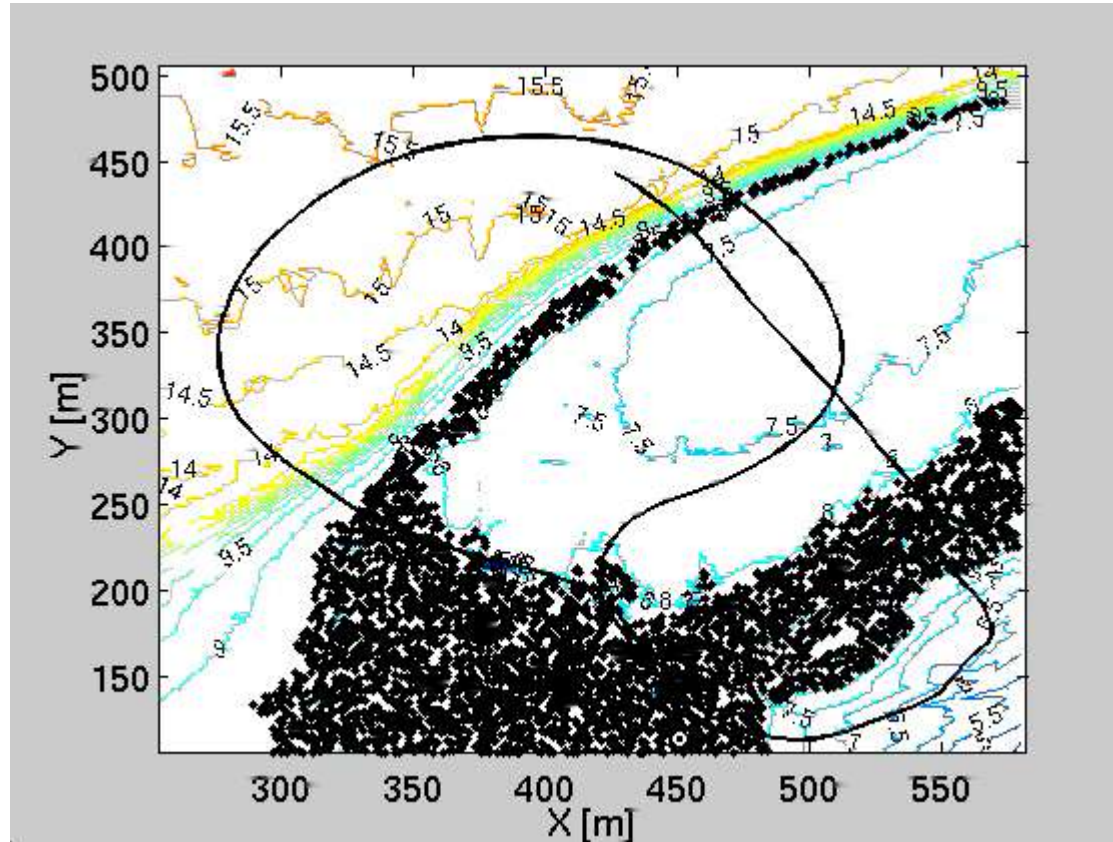
# Particle Filter: t=1







# UW Animation (experimental data)

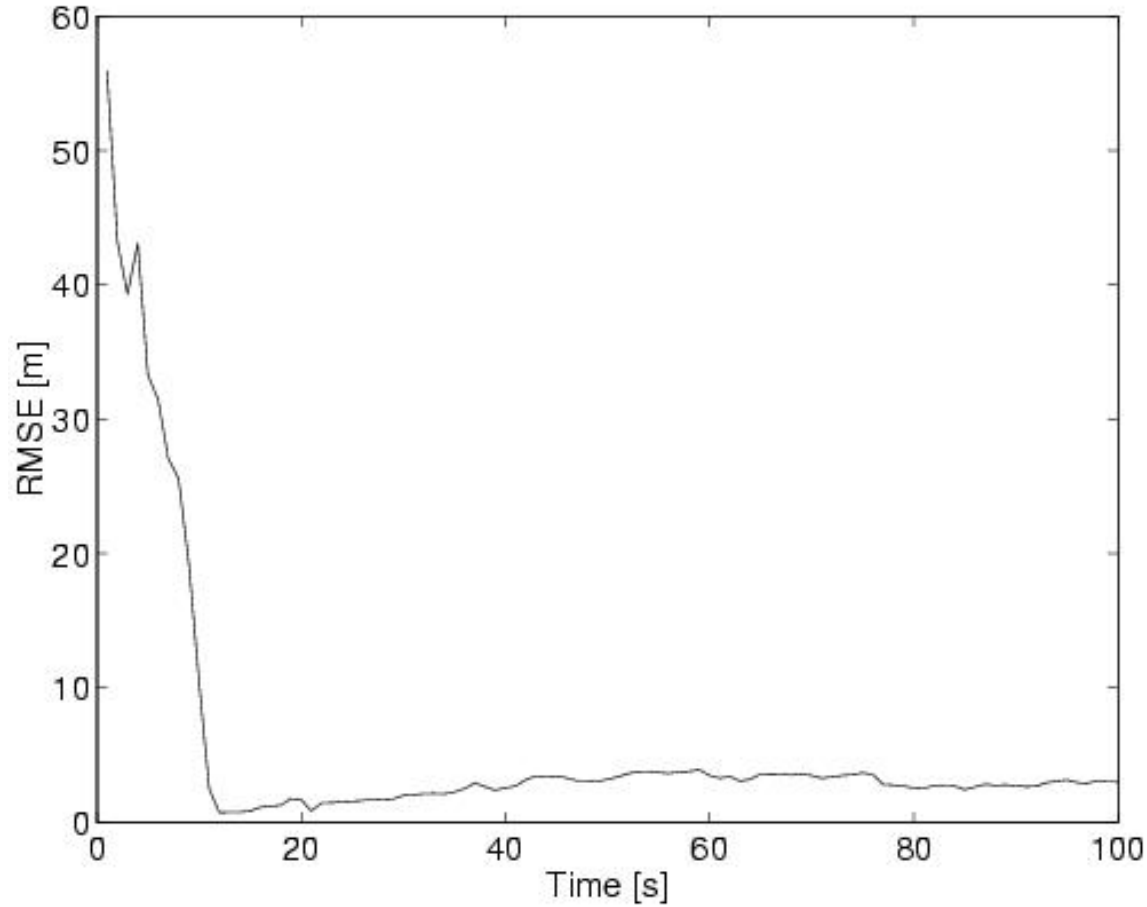


RMSE about 2-10 m

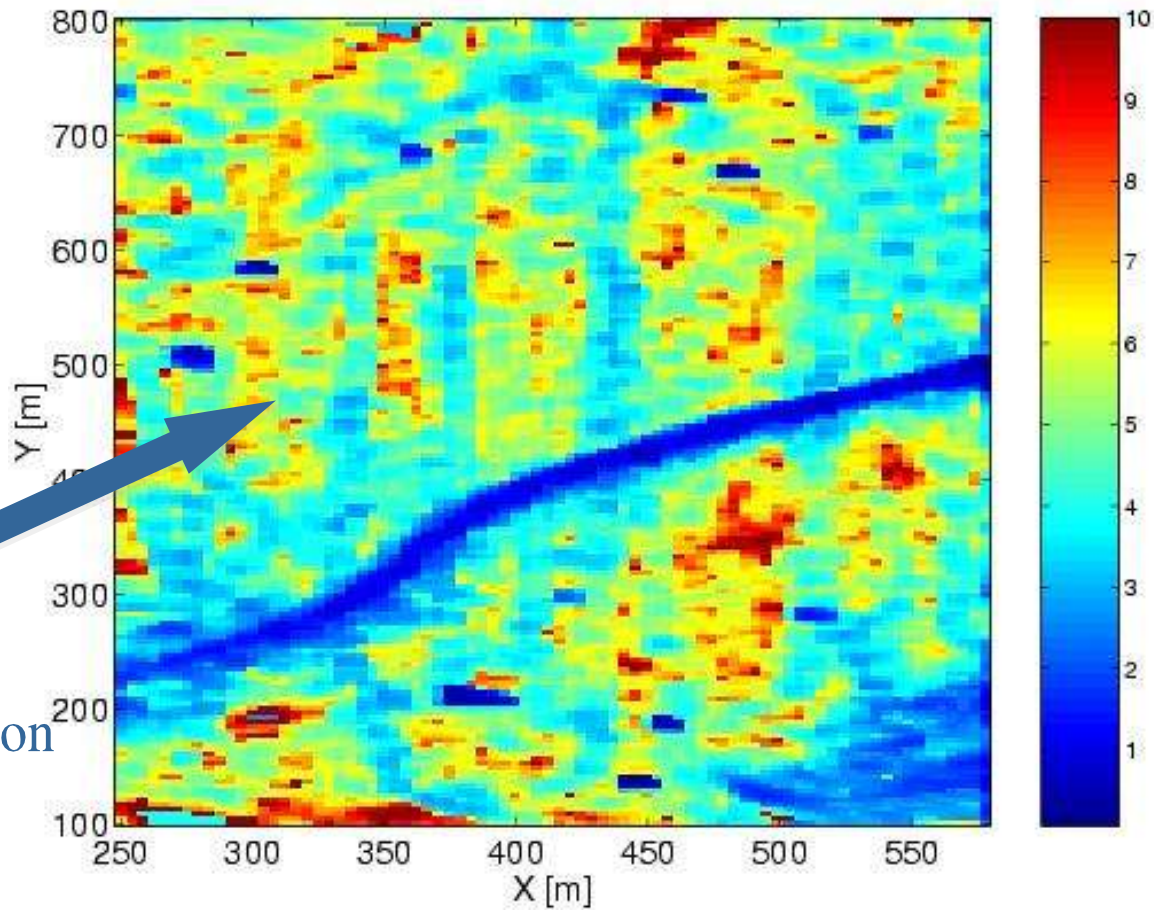




## 50 Monte Carlo Simulations



# CRLB: An Analytic Expression



CRLB for  
each position



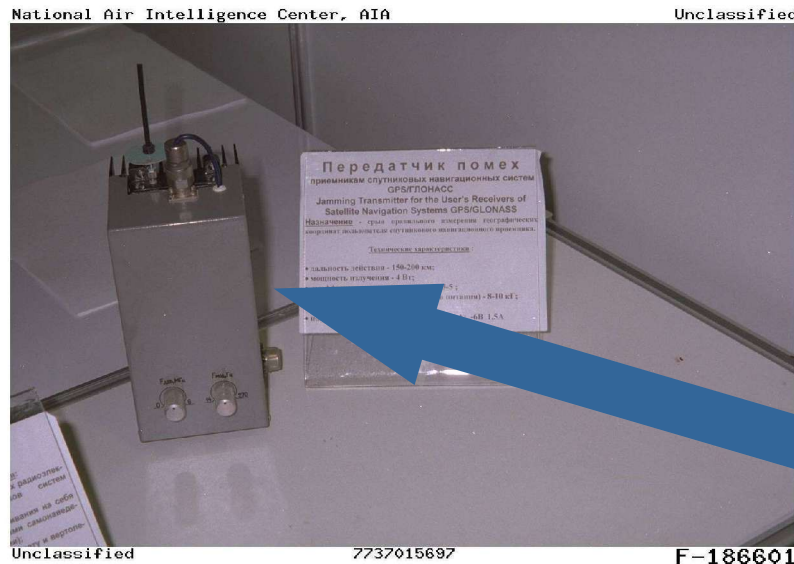
# Map-Aided Surface Navigation

R. Karlsson & F. Gustafsson



# Navigation at Sea using the GPS

- Main positioning sensor at Sea: **GPS**
- American and European authorities have recently published reports on the **need for backup** systems
- Problems: jamming and spoofing



Commercial jammer  
range 150-200 km



# Map-Aided Navigation

Software: Particle Filter

RADAR

GPS

SONAR

OPTIONAL

Patent pending SE-0400264-8

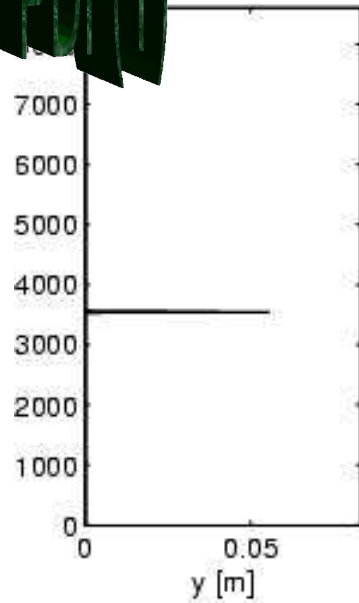


# Surface Navigation

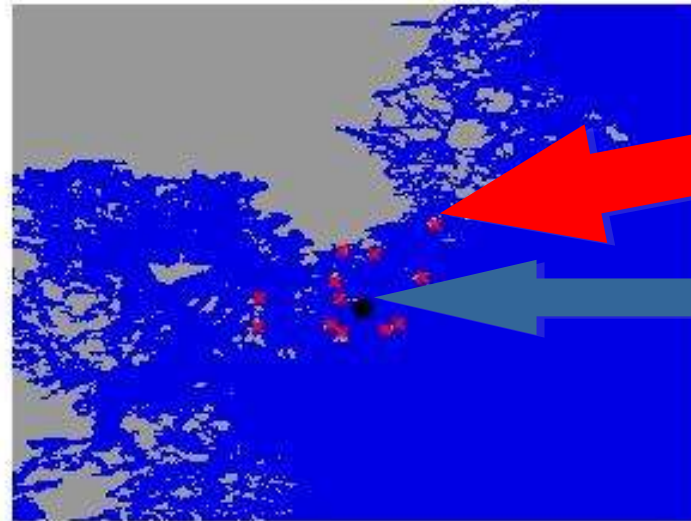


# Surface Navigation: Scenario

PDFEX

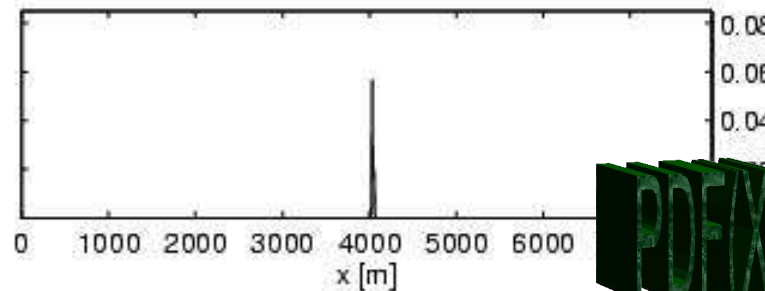


Sample=5



Radar plot

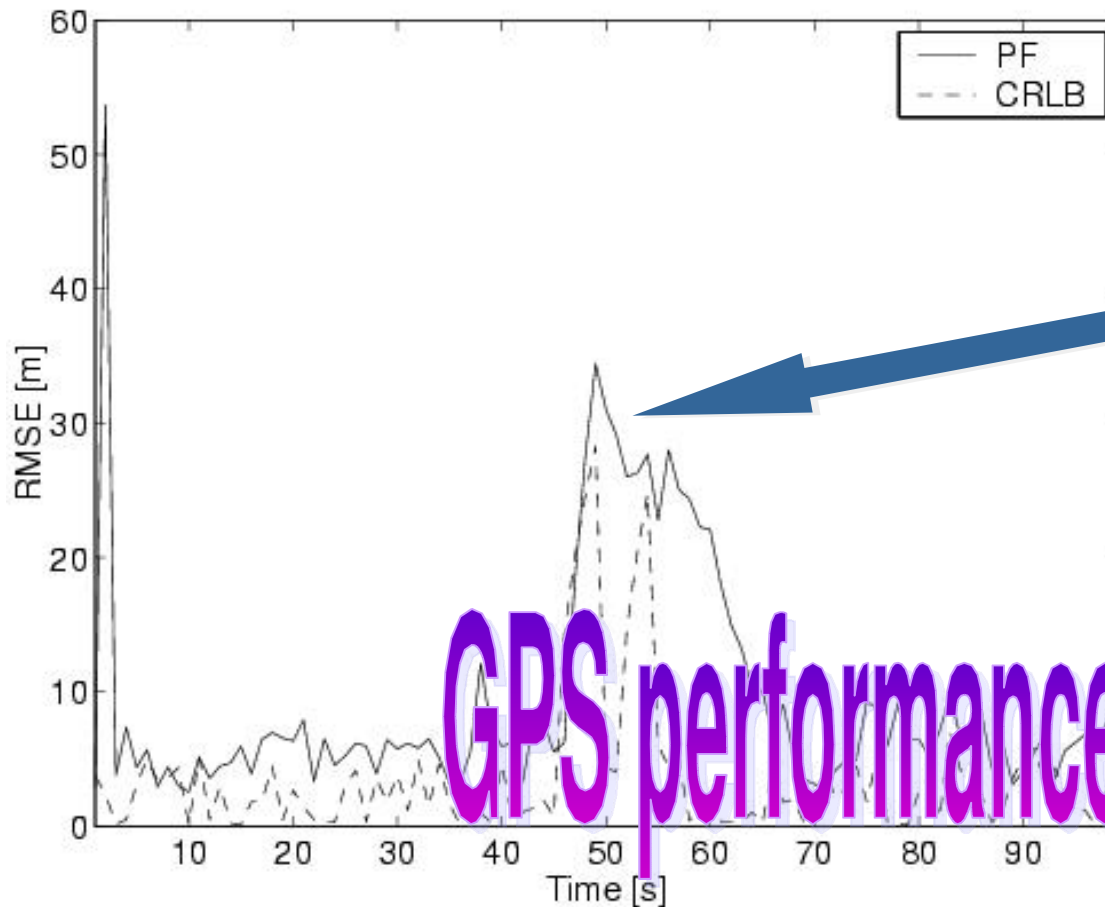
Particles



PDFEX



## 50 Monte Carlo Simulations



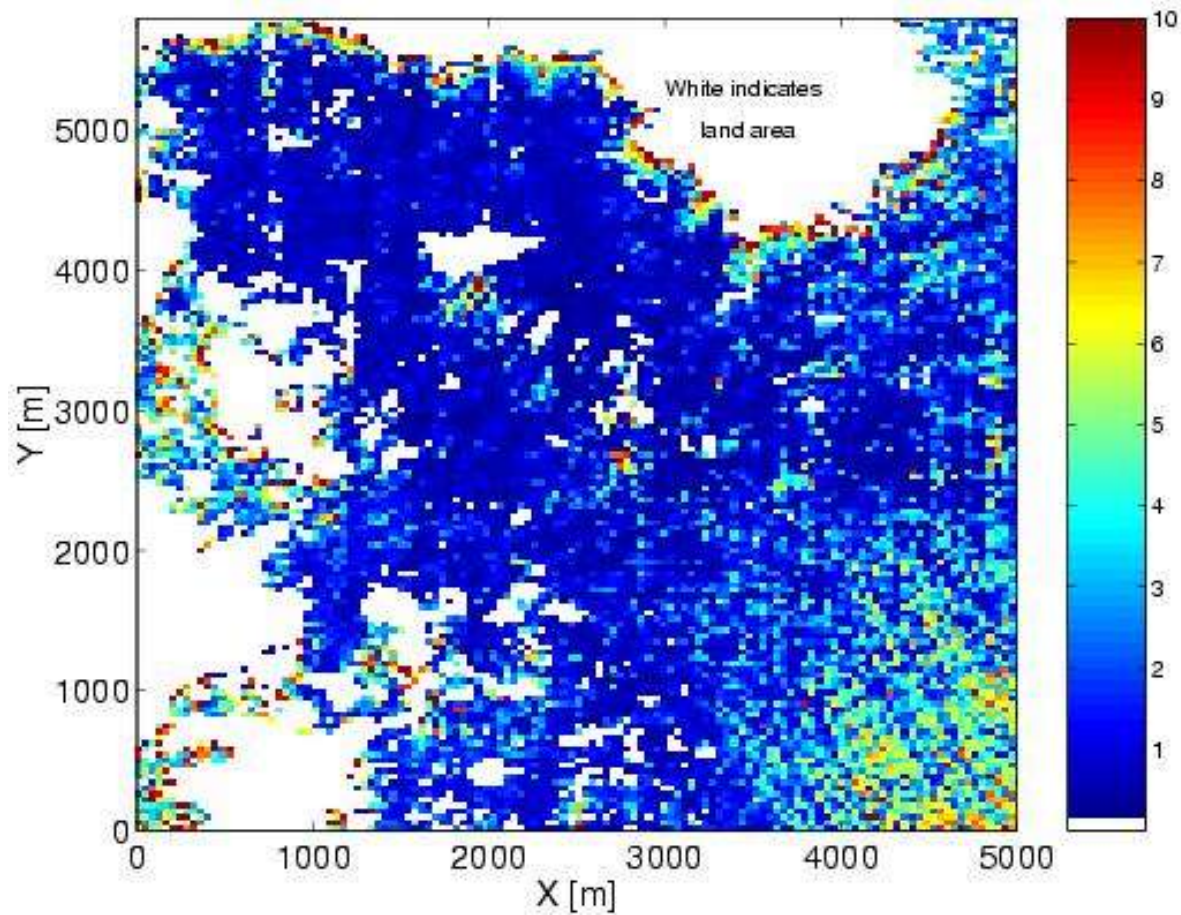
No radar meas.  
available

GPS performance





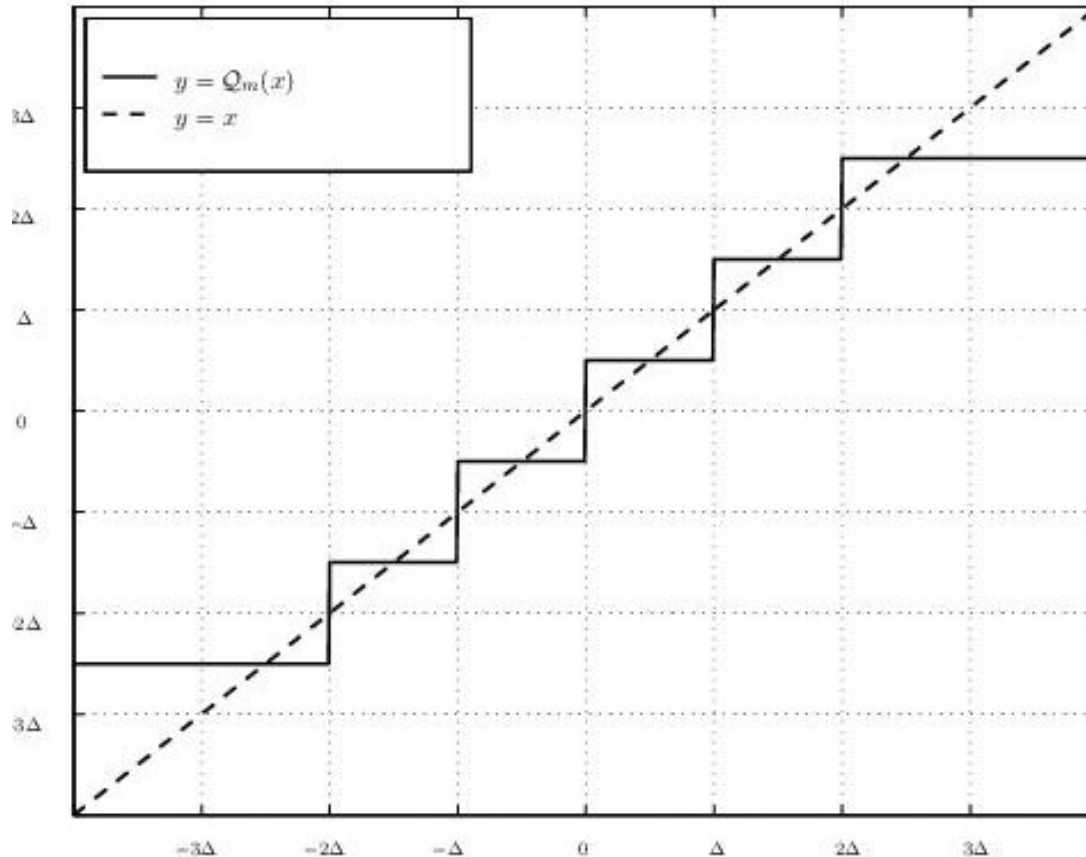
# CRLB: The Analytic Expression



# Quantization

R. Karlsson & F. Gustafsson





## Motivations

- Inexpensive hardware  
Integer, fix-point
- Sensor Networks

$$y_t = Q(x_t + e_t)$$

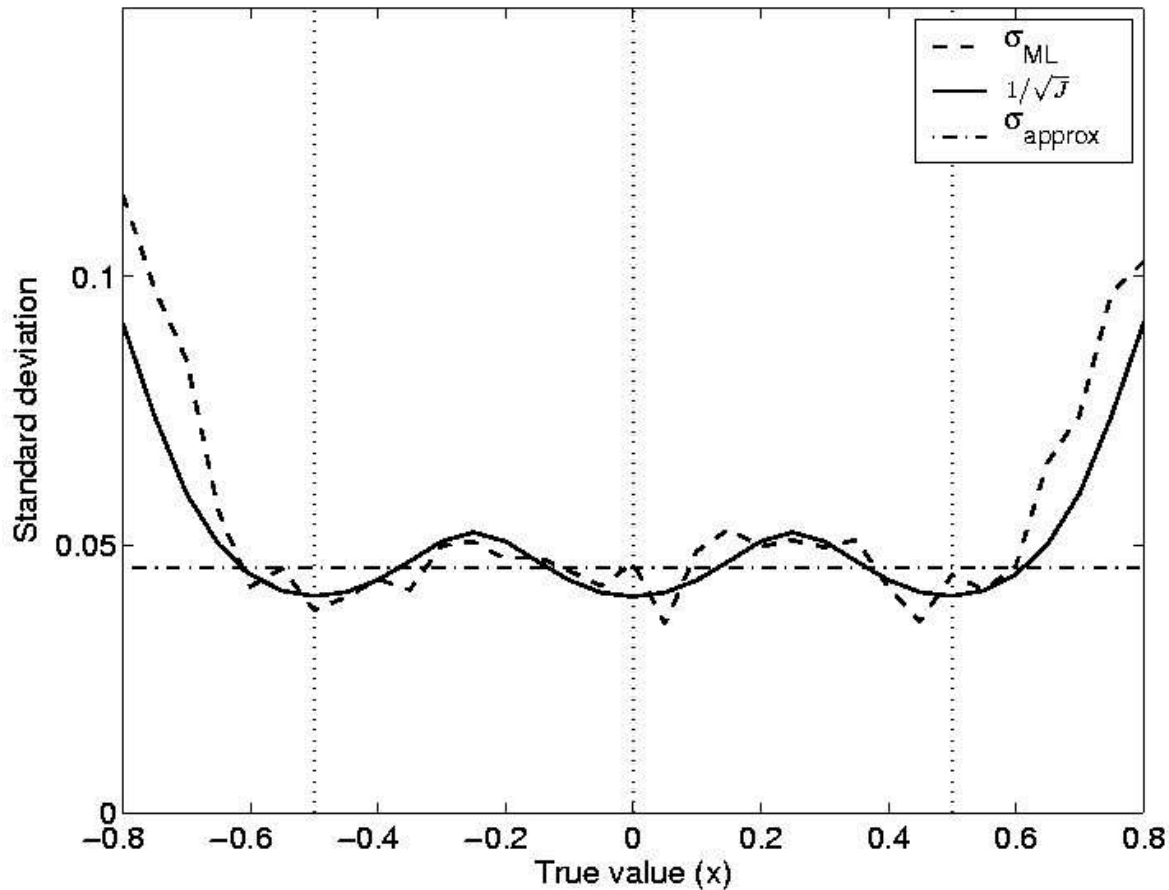


# What's done, some results

- Analytical Results (one-bit, multi-level quantization)
  - ML-estimate
  - CRLB
- Static System
- Dynamic System



# Static: Multi-Level Quantization



$m = 3$  Levels

$$\Delta = \frac{1}{2}$$

MC runs: 20

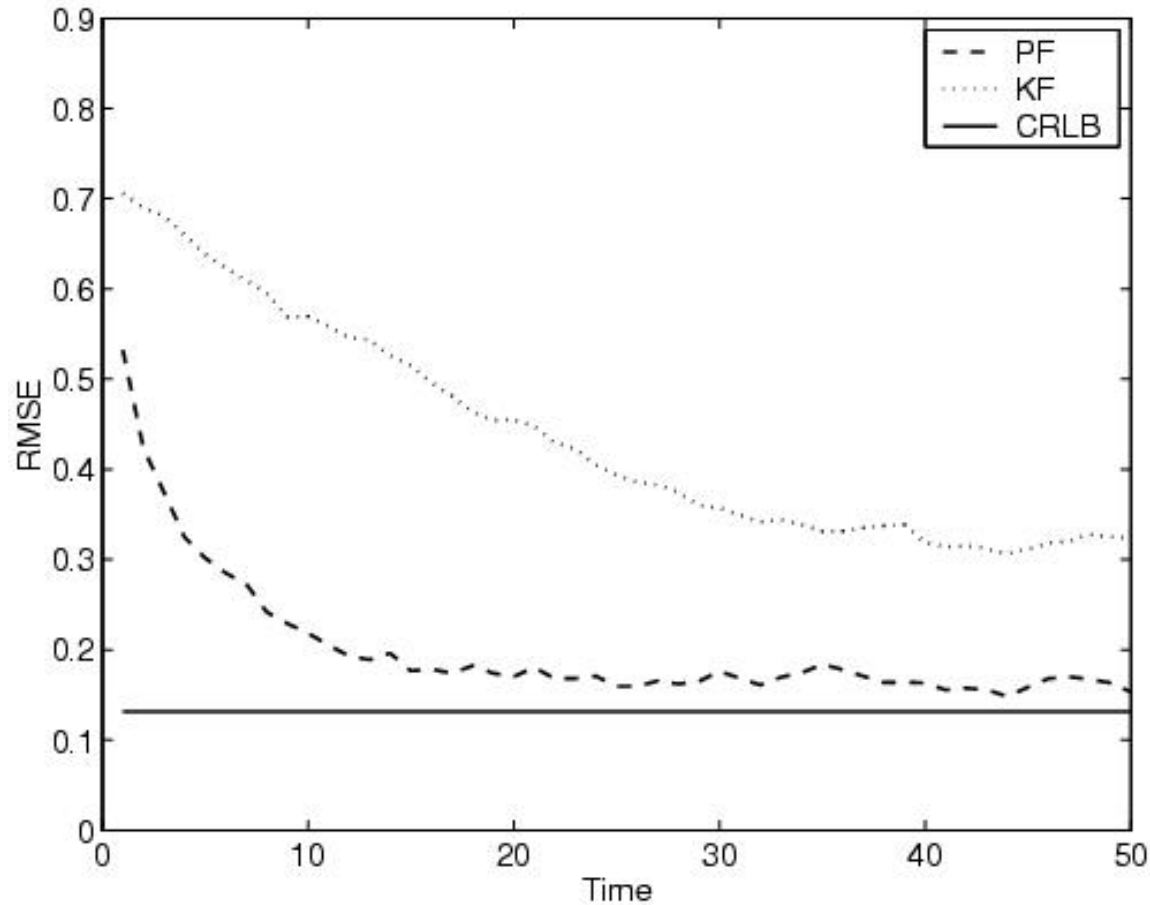
Measurements  $N = 20$

$$\sigma^2 = \frac{\Delta^2}{12} = 0.14^2$$



# Dynamic: One-bit Quantization

Using 5 measurements/time



$$y_t = \text{sign}(x_t + e_t)$$

PF: correct likelihood

KF: approx. likelihood



# The End



# Target Tracking

# Positioning

# Collision Avoidance

# Analysis

